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# Piégeage et refroidissement laser d'atomes et d'ions appliqués à la spectroscopie haute résolution

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## Littérature

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- W. Demtröder, “Laser Spectroscopy“, Springer Verlag, Berlin
- Steven Chu, “The manipulation of neutral particles“, *Reviews of Modern Physics* **70**, 685 (1998).
- Claude N. Cohen-Tannoudji, “Manipulating atoms with photons“, *Reviews of Modern Physics* **70**, 707 (1998).
- William D. Phillips, “Laser cooling and trapping of neutral atoms“, *Reviews of Modern Physics* **70**, 721 (1998).
- Claude N. Cohen-Tannoudji and William D. Phillips, “New Mechanisms for Laser Cooling »; *Phys. Today* 43(10), 33 (1990); doi: 10.1063/1.881239
- <http://www.nobel.se>

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# Plan

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1. Refroidissement laser
2. piège à atomes (mélasses, MOT, fontaines, ...)
3. réseaux atomiques, pièges dipolaires
4. pièges à ions (Paul, Penning, ..)
5. BEC

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## Refroidissement laser

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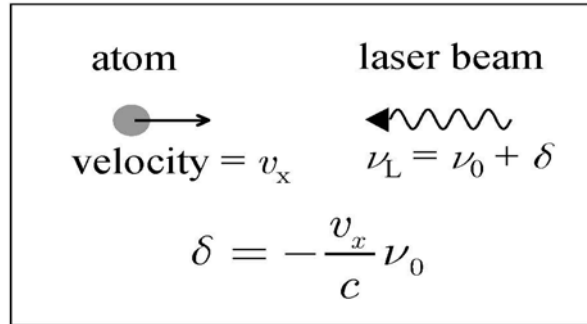
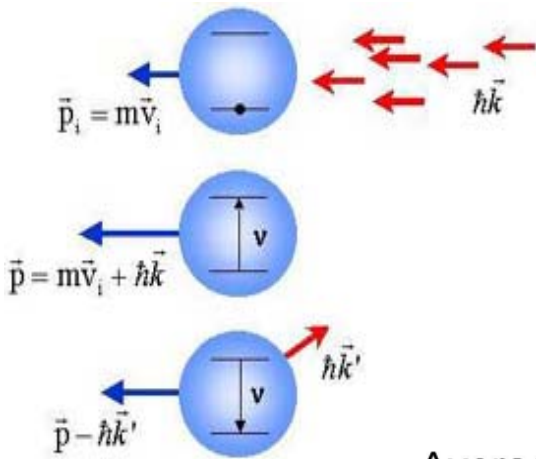
### Depuis 1975...

- **1975 Hänsch/Schawlow and Wineland/Dehmelt** : possibility of laser cooling
- **1978 First demonstration of laser cooling** for trapped ions (Neuhauser et al.; Wineland et al.)
- 1982 First stopping of a thermal beam (Philips & Metcalf)
- **1985 First 3-D cooling (Chu, Hollberg et al.)**  $\approx 240 \mu\text{K}$
- 1987 theory of magneto-optical trap (MOT) (Dalibard et al.)
- 1988 Sub-Doppler cooling (Cohen-Tannoudji et al.)  $\approx 40 \text{ nK}$
- 1995 Laser + evaporative cooling (Anderson, Cornell et al.)  $\approx 20 \text{ nK}$
- 

### *Nobel Prizes*

1989 Paul Dehmelt	ion-trap
<b>1997 Chu, Cohen-Tannoudji, Philips</b>	<b>laser cooling &amp; trapping</b>
2001 Cornell, Ketterle, Wieman	BEC
2005 Glauber, Hall, Hänsch	laser-based precision spectroscopy
2012 Haroche, Wineland	manipulation of individual quantum systems

# Refroidissement laser

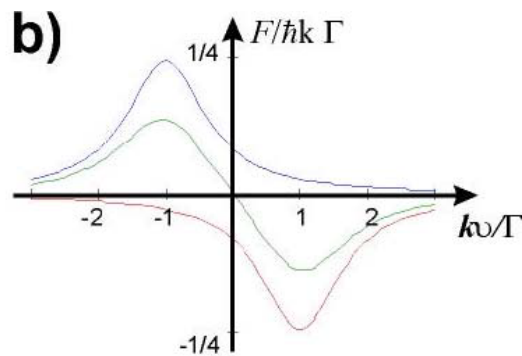
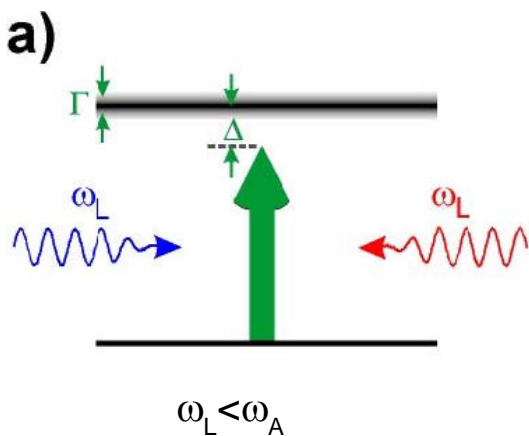


Average momentum kick of  $(-h/\lambda)$  in time  $\tau$

$$F_x = \frac{dp_x}{dt} \sim \frac{\Delta p_x}{\tau} = -\frac{h}{\lambda \tau}$$

<http://archive.nrc-cnrc.gc.ca/eng/projects/inms/fountain-clock.html>

# Refroidissement Doppler



Force de friction  $F = -\alpha v$

$$F(V) = \frac{\hbar k \Gamma}{2} \frac{s_0}{1 + s_0 + 4[\omega_{at} - \omega_L + k_L \cdot V]^2 / \Gamma^2}$$

## Refroidissement Doppler - *limites*

- Nombre de cycle absorption-émission afin de freiner l'atome

$$N_{stop} \approx \frac{initial p_x}{\Delta p_x \text{ per cycle}} \approx \frac{m u_x}{h / \lambda}$$

- le temps nécessaire

$$t_{min} \approx N_{stop} \times 2\tau \approx \frac{m u_x \lambda \tau}{h}$$

- la distance parcourue

$$d_{min} \approx \frac{m \lambda u_x^2}{h}$$

$$k_B T_{min} \sim h \Delta \nu$$

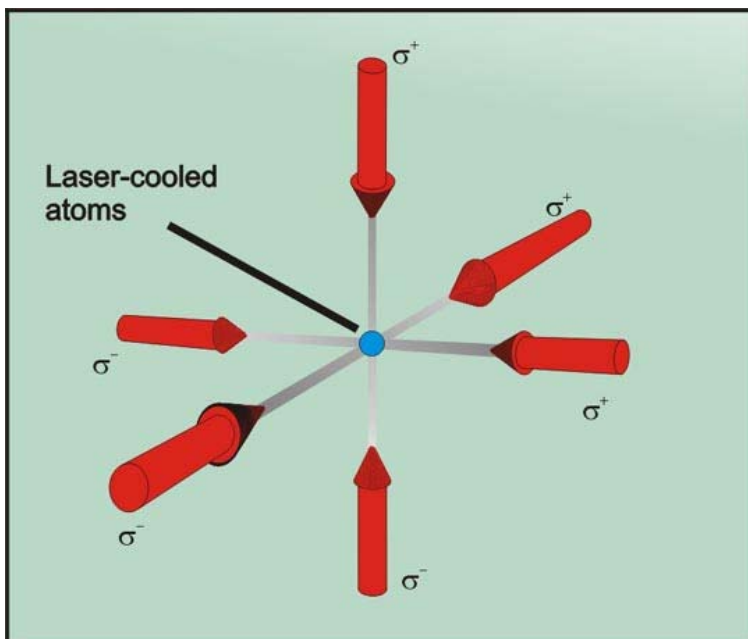
$$T_{min} \approx \frac{\hbar}{2k_B \tau}$$

**Température limite Doppler**

définie par la largeur naturelle de raie

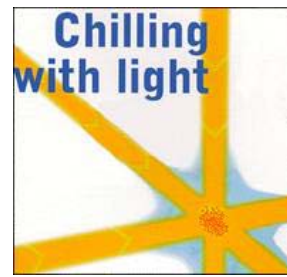
Facteur 2 de l'émission stimulée

## Refroidissement Doppler - 3D



**Mélasse optique**

## 2. Pièges à atomes



### The Nobel Prize in Physics 1997

The Royal Swedish Academy of Sciences has awarded the 1997 Nobel Prize in Physics jointly to

**Steven Chu, Claude Cohen-Tannoudji and William D. Phillips**

for their developments of methods to cool and trap atoms with laser light.



Steven Chu  
Stanford University, Stanford,  
California, USA



Claude Cohen-Tannoudji  
Collège de France and École Normale  
Supérieure, Paris, France

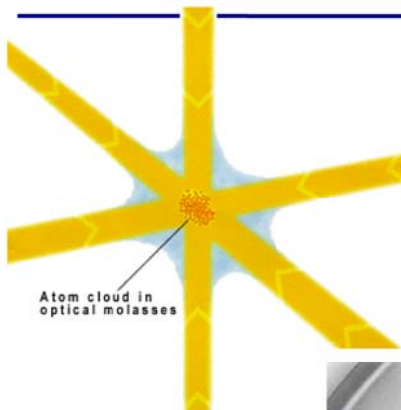


William D. Phillips  
National Institute of Standards and  
Technology, Gaithersburg, Maryland, USA

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## 2. Pièges à atomes – *mélasses optiques*



Atom cloud in  
optical molasses



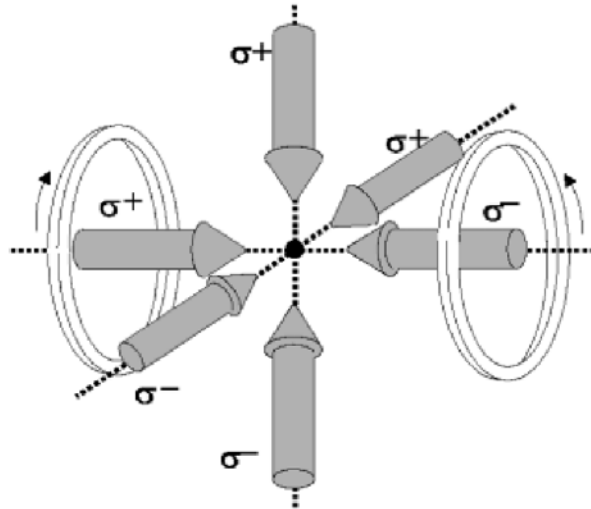
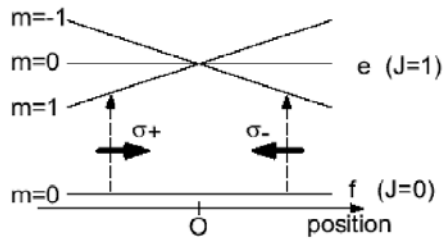
- refroidissement Doppler  
(Hänsch et Schawlow 1975,  
Wineland et Dehmelt 1975)
- une force visqueuse
- ralentissement et confinement
- $V \sim \text{cm}^3$ , fraction de seconde  
(100ms)
- $T \approx 200 \mu\text{K}$

S. Chu, Scientific American, 174, 1992

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## 2. Pièges à atomes - MOT



$$\mathbf{F} = -\alpha \mathbf{v} - k \mathbf{r}$$

mélasse 3D  
effet Doppler

confinement  
effet Zeeman

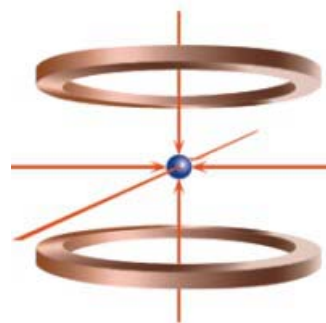
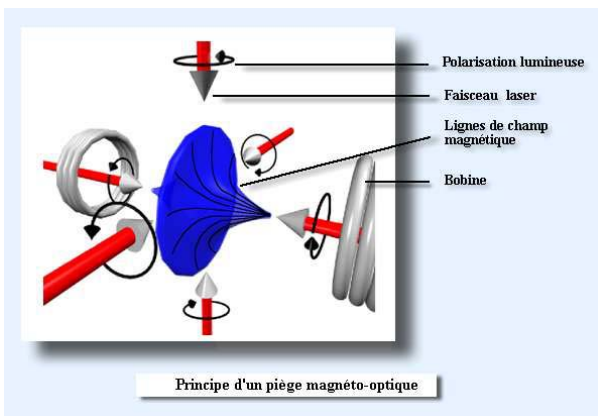
$$b' = 10 \text{ Gauss / cm}$$

$$I = \text{qq mW par faisceau}$$

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## 2. Pièges à atomes - MOT



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## 2. Pièges à atomes - MOT

mesure de la température

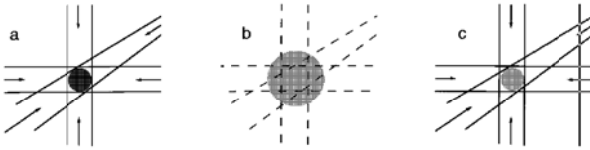
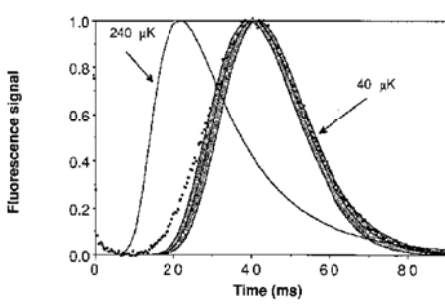
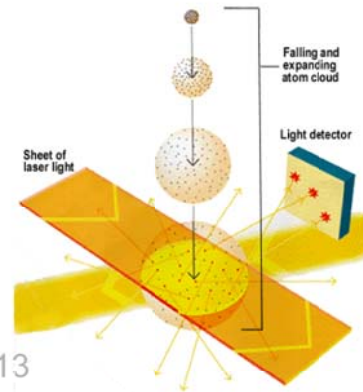
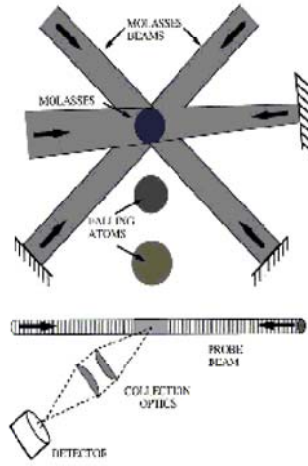


FIG. 13. Release-and-recapture method for temperature measurement.



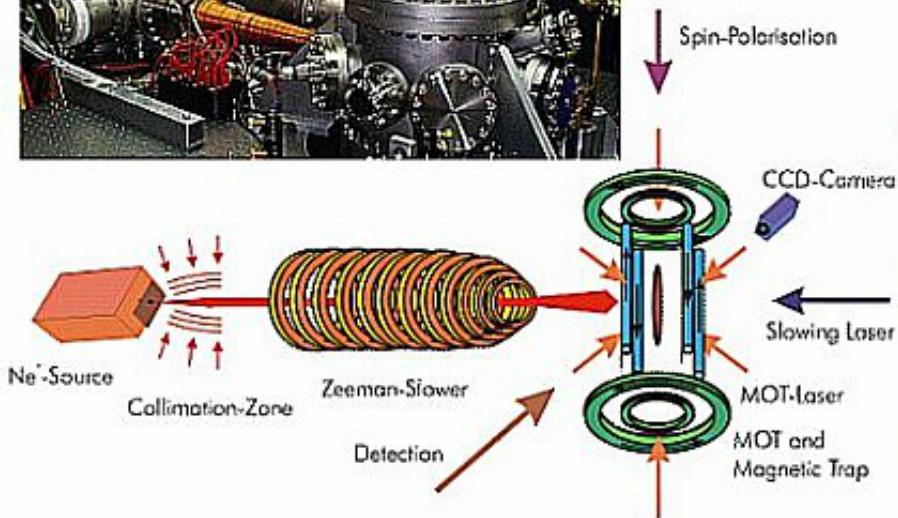
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TOF



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## 2. Pièges à atomes - MOT



MOT néon, IQO, Hannover

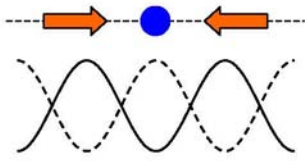


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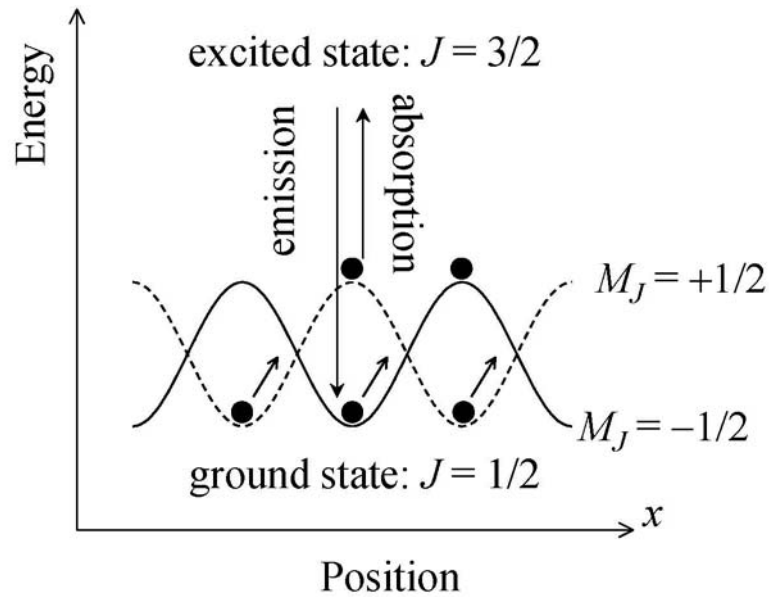
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## 2. Pièges à atomes – polarization gradient cooling

Refroidissement Sisyph



- counter-propagating beams create interference pattern
- Atomic levels shifted by the AC-Stark effect

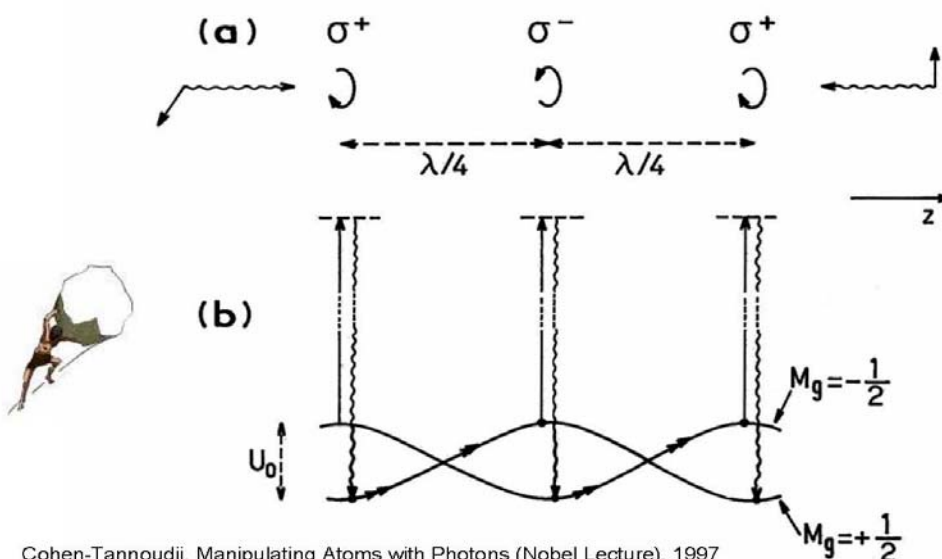


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## 2. Pièges à atomes – polarization gradient cooling

### Sisyphus Cooling



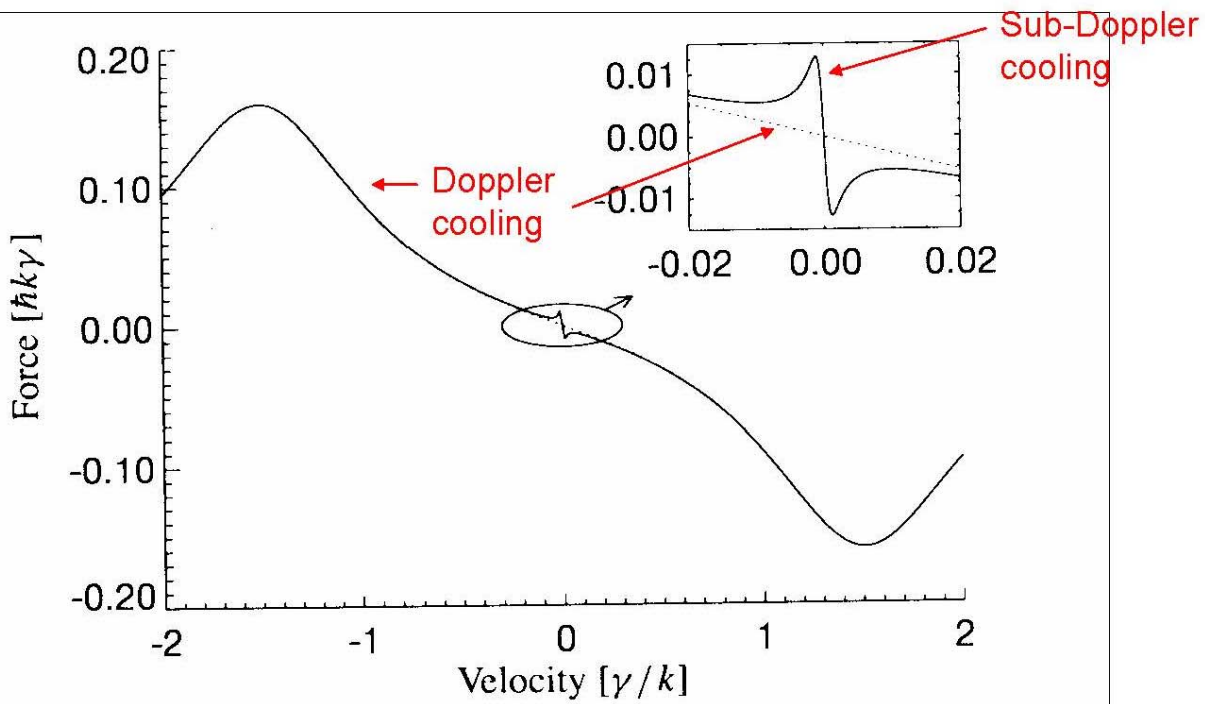
Cohen-Tannoudji, *Manipulating Atoms with Photons* (Nobel Lecture), 1997

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Sous l'effet d'un light shift oscillant



## 2. Pièges à atomes – polarization gradient cooling



H.J. Metcalf, P. van der Straten, *Laser Cooling and Trapping*, Springer, 1999

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## 3. Réseaux atomiques, pièges dipolaires

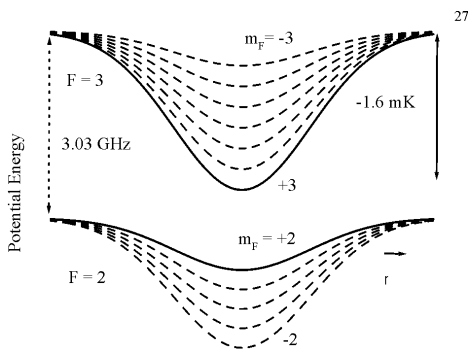


Figure 4.2: AC Stark shift in the focus of a circularly polarized Gaussian laser beam for both hyperfine levels in the  $5s^2$  ground state (under typical experimental parameters, for  $P = 240$  mW. Solid lines indicate the spin states toward which the atoms are driven by absorption of the trapping light.

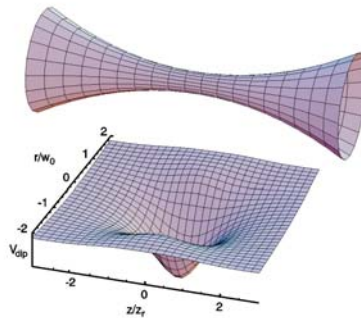


Abbildung 2.9.: Räumliche Verlauf des Dipolpotentials aufgrund des fokussierten Laserstrahls mit  $\omega_0 = 3,5 \mu\text{m}$  und  $\lambda = 850$  nm.

croisement de deux ondes stationnaires

loin de résonance (FORT)

$$U(\rho, z, t) = U_0 \frac{w_0^2}{w(z)^2} \exp\left[-\frac{2\rho^2}{w(z)^2}\right] \cos^2(\pi \Delta v t - kz)$$

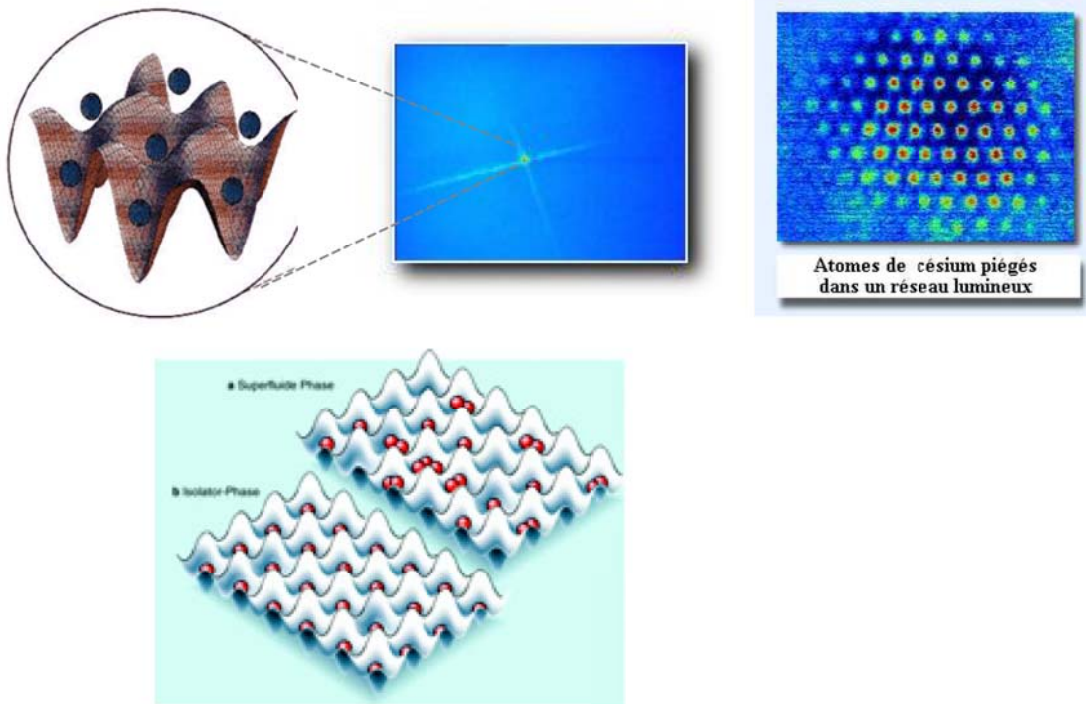
potentiel

$$\text{avec } \lambda = \frac{2\pi}{k}, w(z)^2 = w_0^2 \left(1 + \frac{z^2}{z_0^2}\right), \text{ et } \Delta v = v_1 - v_2$$

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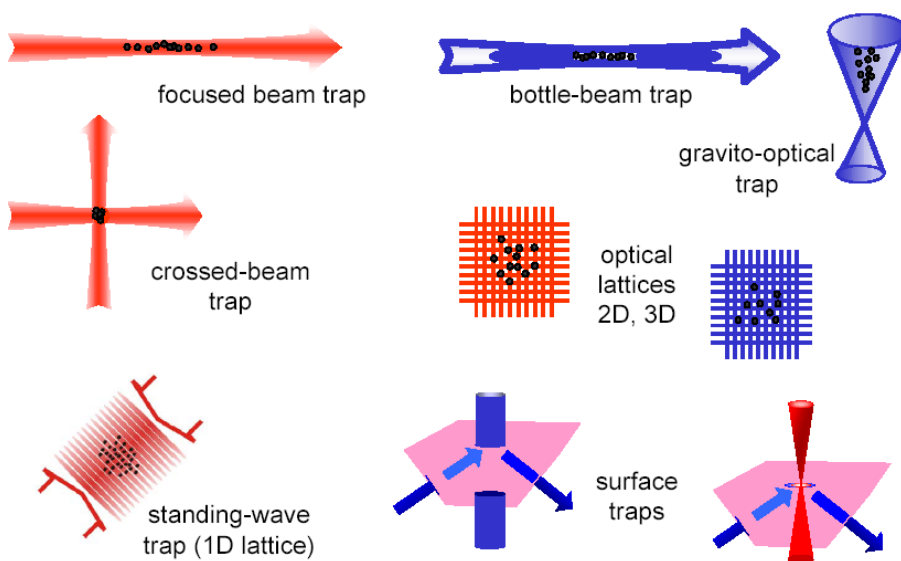
### 3. Réseaux atomiques, pièges dipolaires



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### 3. Réseaux atomiques, pièges dipolaires



**extremely versatile tools → many interesting applications !!!**

D. Guéry-Odelin

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# 4. Pièges à ions

## The Nobel Prize in Physics 1989

The Royal Swedish Academy of Sciences has awarded this year's Nobel Prize in Physics for contributions of importance for the development of atomic precision spectroscopy



**Hans Dehmelt**  
University of Washington  
Seattle, USA

**Wolfgang Paul**  
Universität Bonn  
Federal Republic of  
Germany

**Norman F. Ramsey**  
Harvard University  
Cambridge, USA

for the development of the ion trap technique

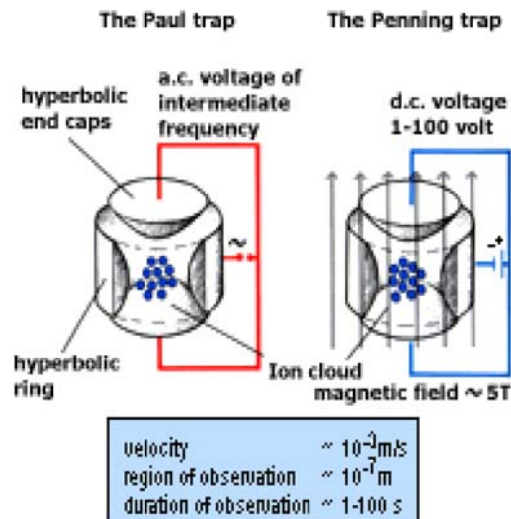
for the invention of the separated oscillatory fields method and its use in the hydrogen maser and other atomic clocks

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# 4. Pièges à ions

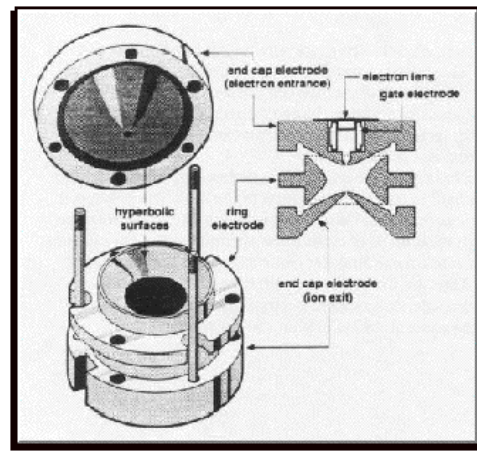
- électrodes métalliques avec application d'un champ
- confinement pendant des durées très longues (*des heures...*)
- permettant des études de grande précision (*temps d'interactions très grands*)
- sélectivité en  $e/m$



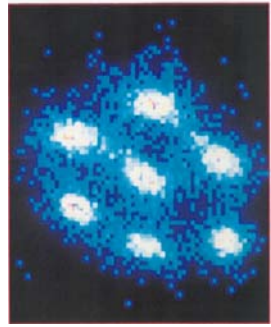
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# Le piège de Paul



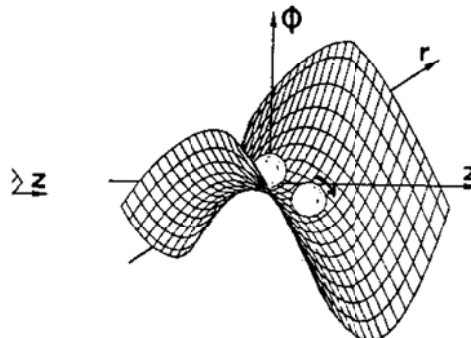
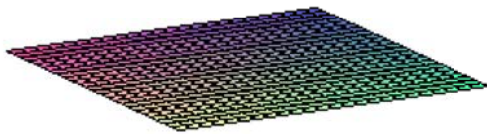
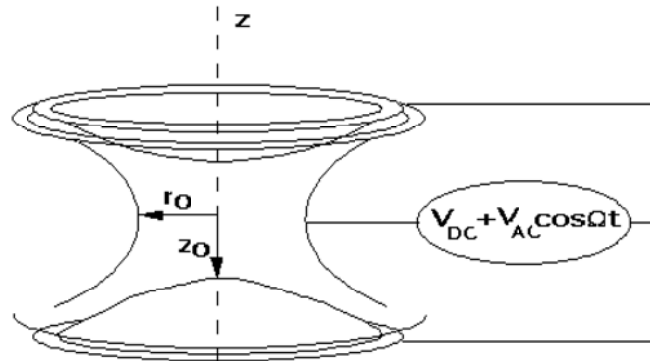
spectroscopie haute résolution et métrologie  
mesures des durées de vie de niveaux atomiques



- ion unique
- sauts quantiques
- lumière non classique
- transition de phase, cristaux coulombiens et chaînes d'ions
- Interférences de deux atomes
- états non classiques
- portes logiques
- mesures de fréquences optiques
- sonde nanométrique
- • •
- spectrométrie de masse
  - outil en chimie structurale
  - collisions réactives lentes et rapides
  - analyse qualitative et quantitative et ses applications

# Le piège de Paul

$$\varphi(x,y,z,t) = (V_{DC} + V_{AC} \cos \Omega t) \frac{x^2 + y^2 + 2z^2}{2r_0^2}$$

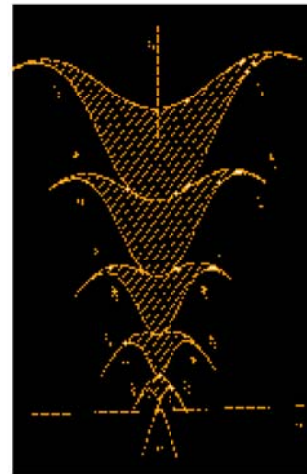


# Le piège de Paul

Mouvement d'une particule chargée régi par un système d'équations de Mathieu (sans interactions avec les autres)

$$u=x,y,z \quad \frac{d^2u}{dt^2} + \frac{\Omega^2}{4}(a_u - 2q_u \cos\Omega t)u = 0$$

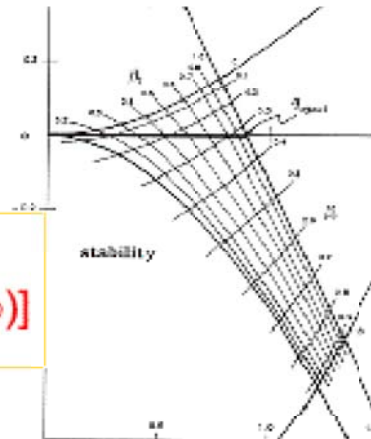
$$a_x = -\frac{a_z}{2} = \frac{8eU_{dc}}{2r_0^2 m \Omega^2}, \quad q_x = -\frac{q_z}{2} = \frac{4eV_{ac}}{2r_0^2 m \Omega^2}$$



Les solutions *stables* sont données par

$$u(t) = u_0 [A_u(t) \cos(\omega_u t + \varphi) + B_u(t) \sin(\omega_u t + \varphi)]$$

$$v_u(t) = u_0 \omega_u [C_u(t) \cos(\omega_u t + \varphi) + D_u(t) \sin(\omega_u t + \varphi)]$$



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# Mouvement des particules

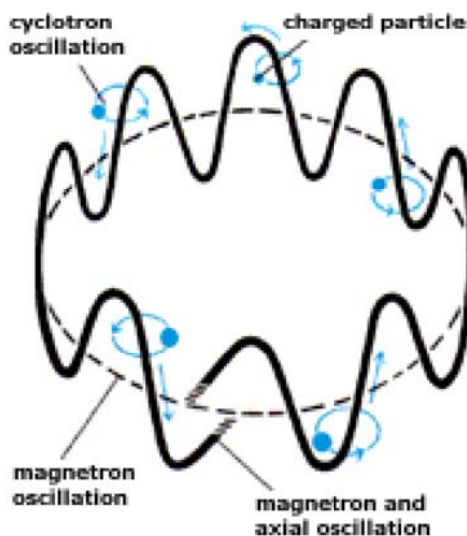
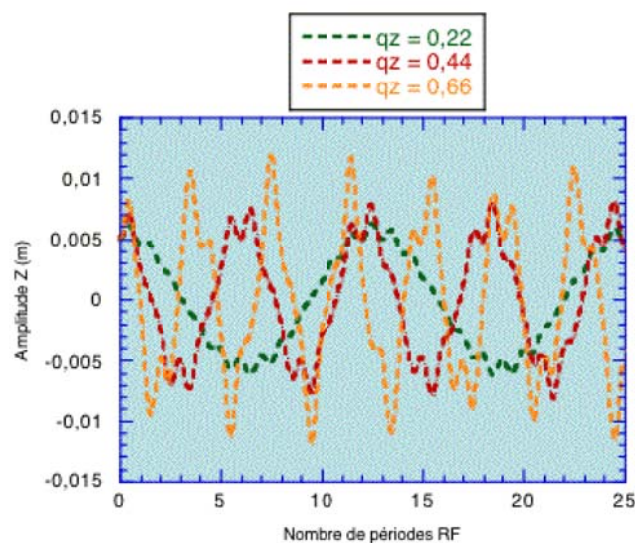
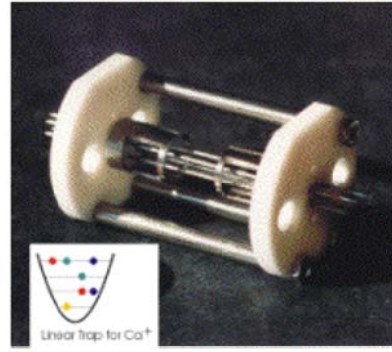
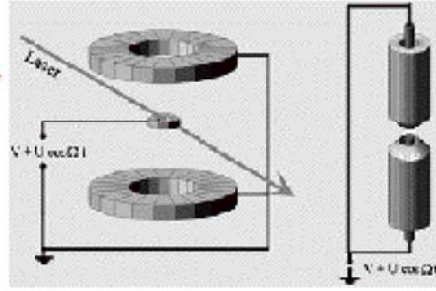
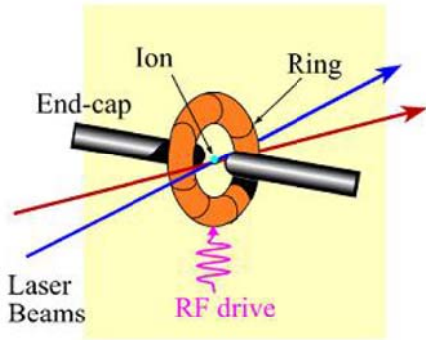


Fig. 9

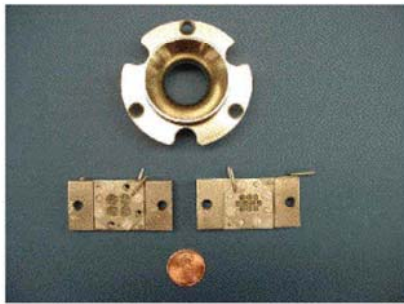


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# Le piège de Paul



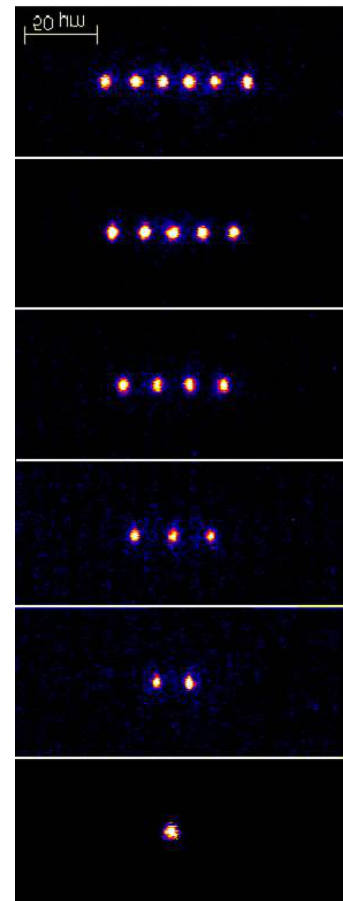
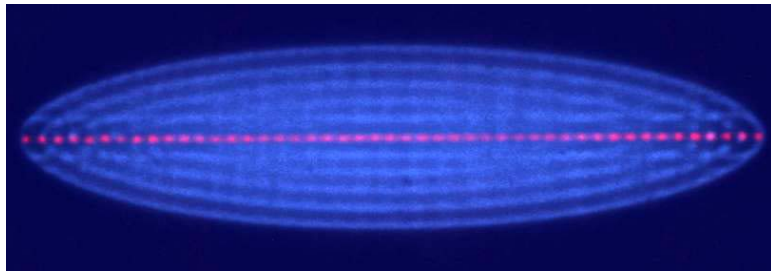
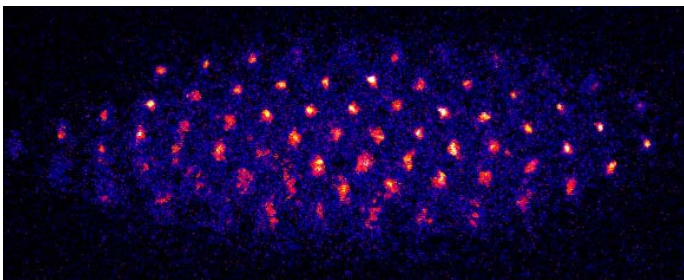
## An Ion Trap



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## Des chaînes

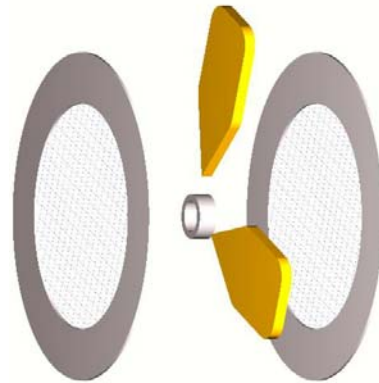
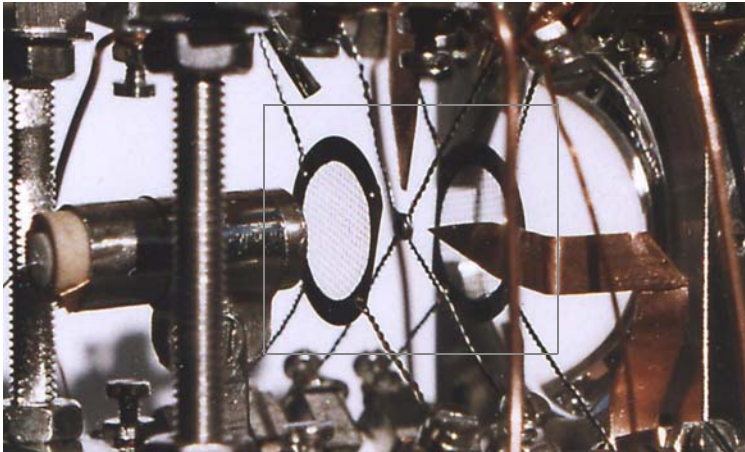


*vers un ion unique*

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# Le piège miniature



## géométrie de *Paul-Straubel*

en molybdène

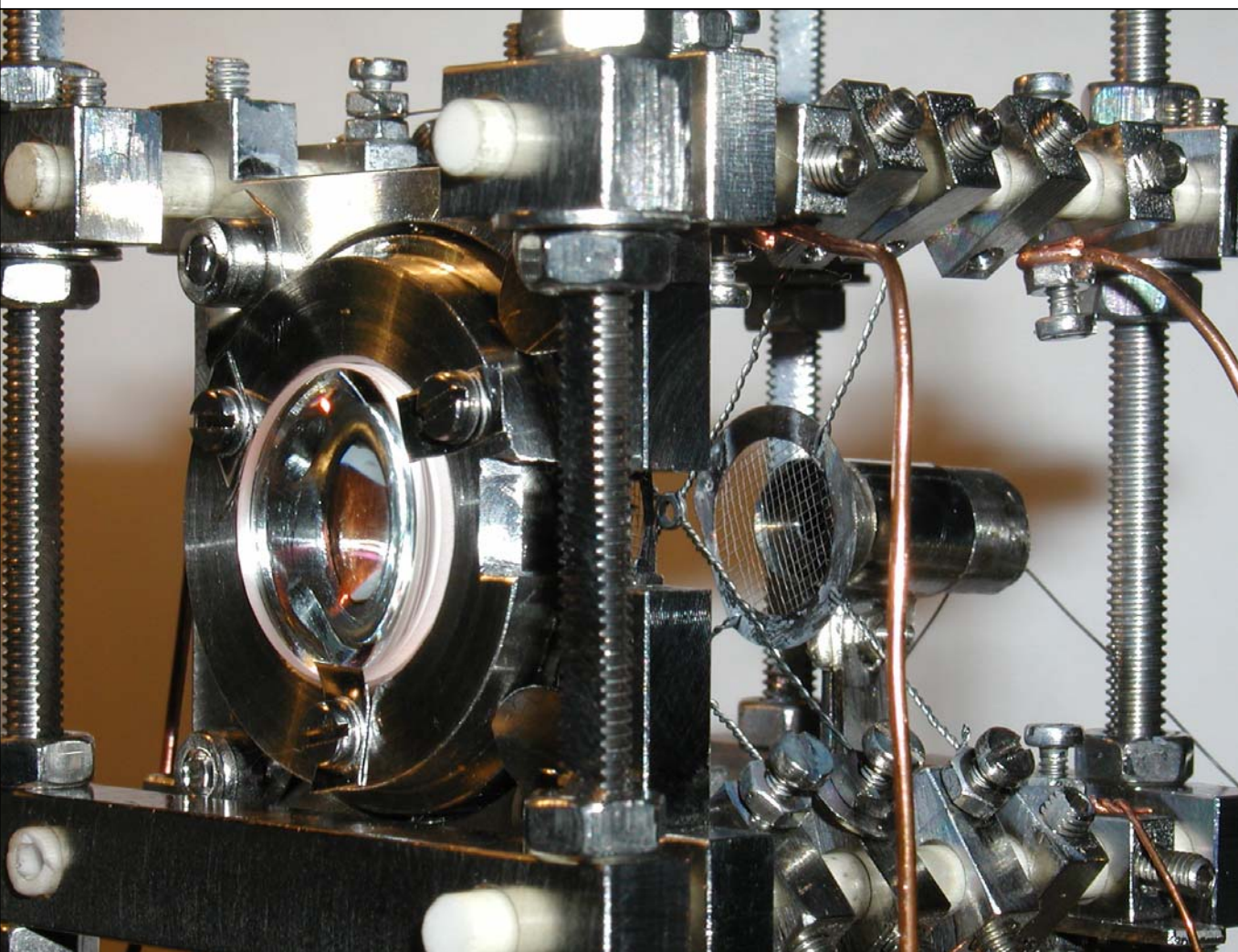
électrodes de compensation en x, y, z (2),  
fréquences séculaires de 1 à 2 MHz.

$r_{\text{int}}=0.7\text{mm}$ ,  $2z_0=0.85\text{mm}$ ,

$\Omega \approx 11.7\text{ MHz}$ ,  $D_{\text{tot}} \approx qq\text{ eV}$

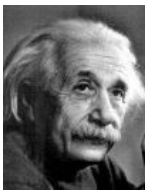
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## 5. Condensats de Bose-Einstein

prédit en 1924 par



A. Einstein



S. Bose

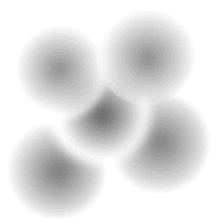
The Nobel Prize in Physics 2001



premier condensat (Rb) créé  
en 1995 au JILA, puis MIT

Eric A. Cornell, Carl E. Wieman, Wolfgang Ketterle

## 5. Condensats de Bose-Einstein



Some very cold atoms



Some atoms in a  
BEC condensate

le « principe d'exclusion de Pauli », interdit à deux fermions identiques d'occuper le même état.

longueur d'onde de Broglie  $\lambda_{dB} = \frac{h}{mv} = \frac{h}{\sqrt{2\pi mk_B T}}$

seuil de condensation  $n\lambda_{dB}^3 = 2.612$

$n$  densité de l'espace de phase

*p.ex. piège dipolaire 0.001-0.005*

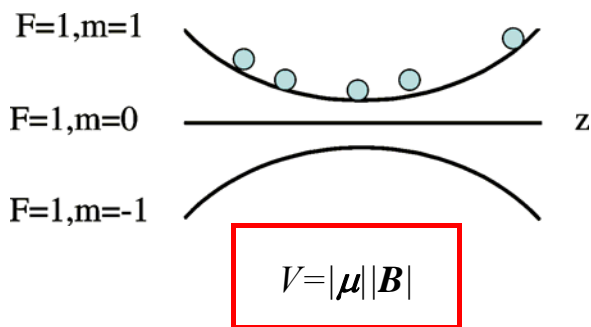


## 5. Condensats de Bose-Einstein

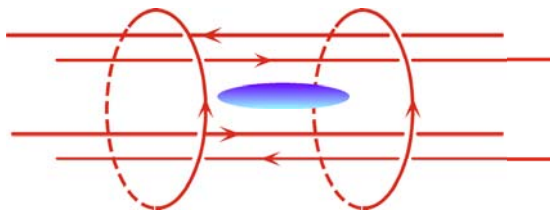
1<sup>ère</sup> étape : MOT  $T = 10 \mu\text{K}$ ,  $N = n\lambda_{\text{dB}}^3$  et énergie de recul !!

2<sup>ème</sup> étape: piège magnétique

minimum local de  $|B|$  + spin polarisation



p.ex. Ioffe-Pritchard trap, profondeur 1 mK

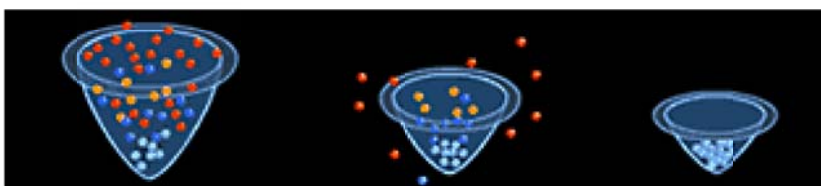


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## 5. Condensats de Bose-Einstein

3<sup>ème</sup> étape: refroidissement évaporatif



redistribution par collisions élastiques

$$N_{\text{in}} \sim 10^9 \text{ at} \quad N_{\text{f}} \sim 10^5 - 10^7 \text{ at} \quad N_{\text{f}} = N_{\text{in}}/100$$

$$T_{\text{in}} \sim \text{qq } 100 \mu\text{K} \quad T_{\text{f}} \sim 1 \mu\text{K} - 500 \text{pK} \quad T_{\text{f}} = T_{\text{in}}/1000$$

$\Rightarrow n\lambda^3 \times 10^7$  !!!      quelques dizaines de secondes

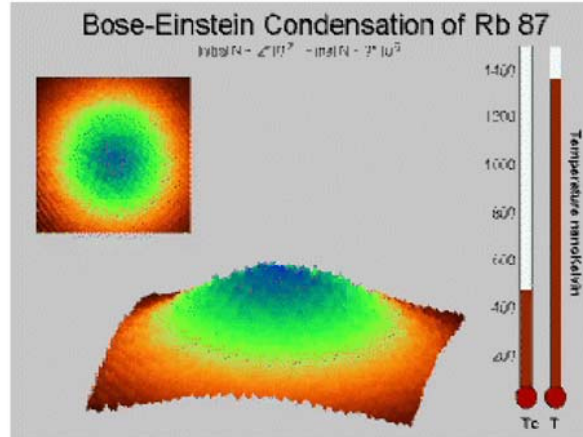
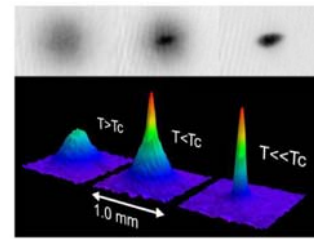
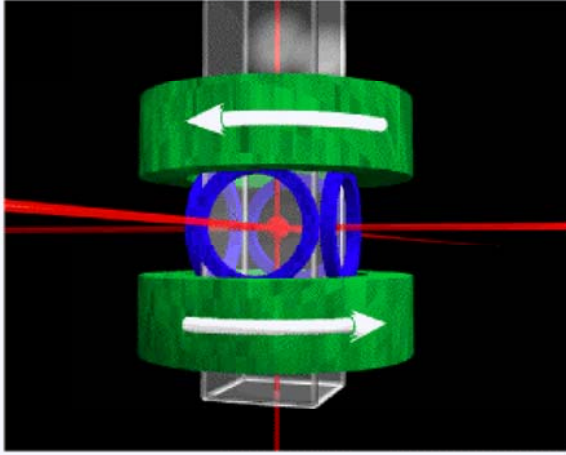
AER – 2012/13

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# 5. Condensats de Bose-Einstein

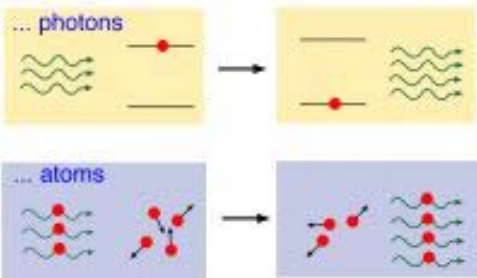
## BEC Apparatus

↑ vacuum pump  
and Rb source

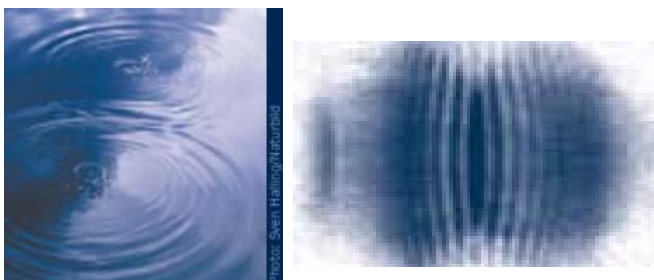


# 5. Condensats de Bose-Einstein

## Stimulated emission/scattering of ...



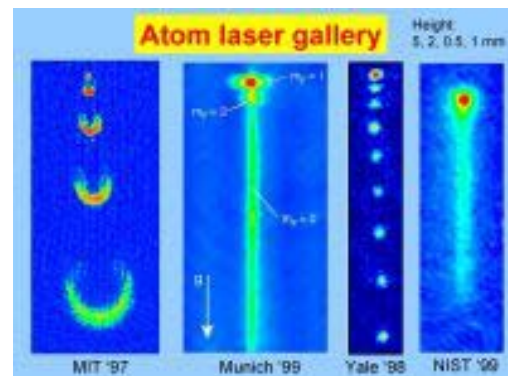
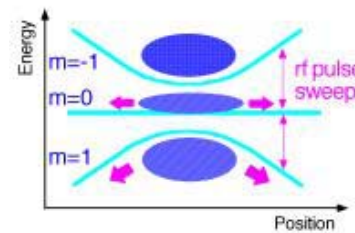
## interférences



## le laser à atomes

An rf output coupler:  $F=1$

$$|BEC\rangle = (|m=-1\rangle)^N \rightarrow (\alpha|m=-1\rangle + \beta|m=0\rangle + \gamma|m=1\rangle)^N$$



## Applications

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- horloges atomiques
- ondes cohérentes de matière (laser à atomes)
- recherche fondamentale

## Synthèse

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types	$\tau_{\text{trap}}$	<b>N</b>	<b>T<sub>limite</sub></b>	$\delta v/v$
cellules		$10^{19} \text{ m}^{-3}$	300K	$10^{-8}$
piège rf	$> h$	1	mK + LD	$< 10^{-18}$
Penning	$> h$		mK	$10^{-6}$
mélasses optiques	$< 100 \text{ ms}$		qq 100 $\mu$ K	$10^{-8}$
MOT	qq s	$10^9$	10 $\mu$ K	$10^{-8}$
fontaines	1s	$10^8$	100 $\mu$ K	$10^{-16}$
réseaux atomiques	s	$10^8$	$\mu$ K	$< 10^{-12}$
BEC	s	$3 \cdot 10^7$	500 pK	??